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Volatility Spillovers Between Crude Oil Futures Returns and Oil Company Stocks Return\textsuperscript{1}

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Abstract

The purpose of this paper is to investigate the volatility spillovers between the returns on crude oil futures and oil company stocks using alternative multivariate GARCH models, namely the CCC model of Bollerslev (1990), VARMA-GARCH model of Ling and McAleer (2003), and VARMA-AGARCH model of McAleer et al. (2008). The paper investigates WTI crude oil futures returns and the stock returns of ten oil companies, which comprise the “supermajor” group of oil companies, namely Exxon Mobil (XOM), Royal Dutch Shell (RDS), Chevron Corporation (CVX), ConocoPhillips (COP), BP (BP) and Total S.A. (TOT), and four other large oil and gas companies, namely Petrobras (PBRA), Lukoil (LKOH), Surgutneftegas (SNGS), and Eni S.p.A. (ENI). Estimates of the conditional correlations between the WTI crude oil futures returns and oil company stock returns are found to be quite low using the CCC model, while the VARMA-GARCH and VARMA-AGARCH models suggest no significant volatility spillover effects in any pairs of returns. The paper also presents evidence of the asymmetric effects of negative and positive shocks of equal magnitude on the conditional variances in all pairs of returns.

Keywords: Multivariate GARCH, Asymmetries, Volatility spillovers, Crude oil futures returns, Oil company stock returns.

JEL Classifications: C22, C32, G17, G32, Q43
1. Introduction

Crude oil is arguably the world’s most influential physical commodity, and plays a prominent role in all economies, so that oil price fluctuations affect the world economy in many different and significant ways. Rising crude oil prices raise the cost of production of goods and services, transportation and heating costs, among others. As a result, it provokes concerns about inflation and restricted discretionary spending of consumer and produces a negative effect to financial markets, consumer confidence, and the macroeconomy (see, for example, Mork (1994), Sadorsky (1999), Lee et al. (2001), Hooker (2002), Hamilton and Herrera (2004), Cunado and Perez de Garcia (2005), Jimenez-Rodriguez and Senchez (2005), Kilián (2008), Cologni and Manera (2008), and Park and Ratti (2008)).

The value of stock prices in an equity pricing model theoretically equals the discounted earnings expectation of companies, or future cash flows. Therefore, oil price shocks influence stock prices through expected cash flows and the discount rate. Since oil is a crucial input for goods and services production, a rise in oil prices without substitute inputs increases production costs, which, in turn, decreases cash flows and stock prices. In addition, rising oil prices affects the discount rate by influencing inflationary pressures, which can also lead central banks to raise interest rates. Thus, corporate investment decisions can be affected directly by changes in the discount rate and changes in stock prices relative to book value. However the direction of the stock price change depends on whether a stock is a producer or consumer of oil and oil-related products. Since most companies in the world market are oil consumers, the performance of oil prices and the stock market may well be negatively correlated.

Several papers have provided an explanation of the oil price and stock market relationship, and the negative impact of oil prices on stock markets (see, for example, Jones and Kaul (1996), Hammoudeh and Aleisa (2002, and 2004), Sadorsky (2008)). However, Maghyereh (2004) does not find a significant impact on stock index returns in 22 emerging economies using a VAR model. This suggests that stock market returns in these economies do not signal shocks in crude oil markets. Surprisingly, there is a limited literature based on the relationship between oil prices and oil company stock prices. There is a positive relationship between the oil price and stock price of oil companies (see, for example, Faff and Brailsford (1999), Sadorsky (2001), Boyer and Filion (2004), El-Sharif
et al. (2005), Basher and Sadorsky (2006), Nandha and Faff (2008), and Henriques and Sadorsky (2008)).

There appears to be volatility spillover patterns that are widespread in financial markets (Milunovich and Thorp (2006)), energy markets, and stock markets (Sadorsky (2004)). A volatility spillover occurs when changes in price or returns volatility in one market produce a lagged impact on volatility in one or more other markets. However, there seems to have been little research of volatility spillovers between the oil and stock markets. Ågren (2006) investigated volatility spillovers from oil prices to stock markets using the asymmetric BEKK model, and presented strong evidence of volatility spillovers in Japan, Norway, U.K. and U.S. stock markets, but quite weak evidence in Sweden.

An assessment of the volatility of oil company stock price returns, and the linkage between oil price volatility and oil company stock price volatility, is crucial for making investment decisions, for policy makers to implement appropriate policies for managing stock markets, and also for financial hedgers, portfolio management, asset allocators, and other financial analysis. With oil and gas being one of the largest industries in the world, different companies and business are involved in different chains of production, distillation and distribution. It is surprisingly that none of these papers has yet examined the relationship between crude oil futures returns volatility and oil company stock price volatility.

In order to model volatility spillovers, there are several conditional volatility models which specify the risk of one asset as depending dynamically on its own past risk and on the past risk of other assets (see, for example, McAleer (2005)). Even though the multivariate VARMA-GARCH model of Ling and McAleer (2003) and VARMA-AGARCH model of McAleer et al. (2009) assume constant conditional correlations, they do not suffer from the “curse of dimensionality” when compared with the VECH and BEKK models (see, for example, Caporin and McAleer (2009)). On the other hand, in order to capture the dynamics of time-varying conditional correlations, a recently developed model is the generalized autoregressive conditional correlation (GARCC) of McAleer et al. (2008).

The purpose of the paper is to examine volatility spillovers between crude oil futures returns and oil company stock returns for the major oil companies. This issue is examined empirically using the VARMA-GARCH and VARMA-AGARCH models. The
empirical results of the paper may shed light on the importance of crude oil returns on oil company stock returns.

The remainder of the paper is organized as follows. Various multivariate conditional volatility models are discussed in Section 2. The data sources and sample evidence are described in Section 3, and the empirical results are analyzed in Section 4. Some concluding remarks are given in Section 5.

2. Methodology

The purpose of this section is to present alternative multivariate conditional volatility models, including a discussion of spillover effects, in which the conditional variance of returns depends dynamically on past unconditional shocks and the past conditional variance of each asset in the portfolio. The VARMA-GARCH model of Ling and McAleer (2003) assumes symmetry in the effects of positive and negative shocks of equal magnitude on the conditional volatility, and is given by

\[
Y_t = E(Y_t | F_{t-1}) + \varepsilon_t, \tag{1}
\]

\[
\Phi(L)(Y_t - \mu) = \Psi(L)\varepsilon_t, \tag{2}
\]

\[
\varepsilon_t = D_t \eta_t, \tag{3}
\]

\[
H_t = W_t + \sum_{l=1}^{r} A_l \tilde{\varepsilon}_{t-l} + \sum_{l=1}^{s} B_l H_{t,i-l} \tag{4}
\]

where \( Y_t = (y_{t1}, \ldots, y_{tm})' \), \( F_{t-1} \) is the past information available to time \( t \), \( m \) is the number of returns to be analyzed, \( t = 1, \ldots, n \), \( L \) is the lag operator, \( \Phi(L) = I_m - \Phi_1 L - \ldots - \Phi_p L^p \) and \( \Psi(L) = I_m - \Psi_1 L - \ldots - \Psi_q L^q \) are polynomials in \( L \), \( D_t = \text{diag}(h_{t,i,j}^{1/2}) \), \( \eta_t = (\eta_{t1}, \ldots, \eta_{tm})' \) is a sequence of independently and identically (iid) random vectors, \( H_t = (h_{t1}, \ldots, h_{tm})' \), \( W_t = (\omega_{t1}, \ldots, \omega_{tm})' \), \( \tilde{\varepsilon}_t = (\varepsilon_{t1}^2, \ldots, \varepsilon_{tm}^2)' \), \( A_l \) and \( B_l \) are \( m \times m \) matrices with typical elements \( \alpha_{ij} \) and \( \beta_{ij} \), respectively, for \( i, j = 1, \ldots, m \), and \( A_l \) and \( B_l \) represent the ARCH and GARCH effects, respectively.
Spillover effects, or the dependence of the conditional variance between WTI crude oil futures returns and oil company stock returns, are given in the conditional volatility for each return in the portfolio. Based on equation (3), the VARMA-GARCH model also assumes that the matrix of conditional correlations is given by \( E(\eta_\tau^t) = \Gamma \). If \( m = 1 \), equation (4) reduces to the univariate GARCH model of Bollerslev (1986), namely:

\[
h_t = \omega + \sum_{i=1}^{m} \alpha_i \varepsilon_{t-i}^2 + \sum_{i=1}^{m} \beta_i h_{t-i}^2 \tag{5}
\]

An extension of the VARMA-GARCH model to accommodate asymmetric impacts of positive and negative shocks is given by the VARMA-AGARCH model of McAleer et al. (2009), which captures asymmetric spillover effects from each return. An extension of (4) to accommodate asymmetries with respect to \( \varepsilon_t \) is given by

\[
H_t = W + \sum_{i=1}^{l} A_i \varepsilon_{t-i}^2 + \sum_{i=1}^{l} C_j I(\eta_{t-i}) \varepsilon_{t-i} + \sum_{i=1}^{l} B_l H_{t-i} \tag{6}
\]

in which \( \varepsilon_t = \eta_t \sqrt{h_t} \) for all \( i \) and \( t \), \( C_i \) are \( m \times m \) matrices, \( I(\eta_{t-i}) \) is an indicator variable, and \( I(\eta_t) = \text{diag}(I(\eta_t)) \) is an \( m \times m \) matrix, such that

\[
I(\eta_t) = \begin{cases} 
0, & \varepsilon_t > 0 \\
1, & \varepsilon_t \leq 0 
\end{cases} \tag{7}
\]

If \( m = 1 \), equation (4) reduces to the asymmetric univariate GARCH, or GJR, model of Glosten et al. (1992):

\[
h_t = \omega + \sum_{j=1}^{r} \left( \alpha_j + \gamma_j I(\eta_{t-j}) \right) \varepsilon_{t-j}^2 + \sum_{j=1}^{r} \beta_j h_{t-j} \tag{8}
\]

If \( C_j = 0 \) with \( A_i \) and \( B_l \) being diagonal matrices for all \( l \), then VARMA-AGARCH reduces to:
which is the constant conditional correlation (CCC) model of Bollerslev (1990). As given in equation (7), the CCC model does not have asymmetric effects of positive and negative shocks on conditional volatility, or volatility spillover effects across different financial assets, so it is intrinsically univariate in nature. From (2), the conditional correlation is $\varepsilon_i | \mathbf{F}_{t-1} = D_t \eta_t \eta_t' \mathbf{D}_t$, and the conditional covariance matrix is given by

$$E(\varepsilon_i \varepsilon_i' | \mathbf{F}_{t-1}) = \Omega_t = \mathbf{D}_t \Gamma \mathbf{D}_t.$$ (10)

Therefore, the conditional correlation matrix is defined as $\Gamma = \mathbf{D}_t^{-1} \Omega_t \mathbf{D}_t^{-1}$. The parameters in model (1), (4), (6) and (9) can be obtained by maximum likelihood estimation (MLE) using a joint normal density, namely

$$\hat{\theta} = \arg\min_{\theta} \frac{1}{2} \sum_{t=1}^{n} \left( \log |Q_t| + \varepsilon_t Q_t^{-1} \varepsilon_t \right)$$ (11)

where $\theta$ denotes the vector of parameters to be estimated via the conditional log-likelihood function, and $|Q_t|$ denotes the determinant of $Q_t$, the conditional covariance matrix. When $\eta_t$ does not follow a joint multivariate normal distribution, the appropriate estimators are defined as Quasi-MLE (QMLE).

The conditional correlations may be made dynamic, as given in the extension of the above models to multivariate conditional and stochastic volatility models, for which see McAleer et al. (2008), and Asai and McAleer (2009), respectively.

3. Data

In this paper, we focus on modelling volatility spillovers between crude oil futures returns in the WTI market and ten oil company stock returns. Six of these oil companies are called “Supermajor”, namely the six largest non state-owned energy companies, which
comprise Exxon Mobil (XOM, US), Royal Dutch Shell (RDS, The Netherlands), Chevron Corporation (CVX, US), ConocoPhillips (COP, US), BP (BP, UK) and Total S.A. (TOT, French), with the next four being Petrobras (PBRA, Brasil), Lukoil (LKOH, Russia), Surgutneftegas (SNGS, Russia), and Eni S.p.A. (ENI, Italy).

All 3,202 price observations are from 14 November 1996 to 20 February 2009. The data are obtained from DataStream database services, and are expressed in local currencies, with the exception of WTI crude oil futures prices, which are denominated in USD per barrel. The returns of the daily futures prices for WTI, and for the ten oil company stock prices, are given in Figures 1 and 2, respectively. As the Augmented Dickey-Fuller (ADF) and Phillips-Perron (PP) test provide large negative values in all cases, all the individual returns series are stationary. The empirical results of the unit root tests for WTI crude oil futures return and ten oil company stock price returns are available from the authors on request.

4. Empirical results

As the univariate ARMA-GARCH model is nested in the VARMA-GARCH model, and ARMA-GJR is nested in VARMA-AGARCH, with the conditional variances specified as in (5) and (8), the univariate ARMA-GARCH and ARMA-GJR models are estimated. It will be appropriate to extend the univariate models to their multivariate counterparts if the properties of the univariate models are satisfied. The coefficients in the conditional variance equations from the ARMA(1,1)-GARCH(1,1) model are significant, both in the short and long run. However, the coefficients in the conditional variance of ARMA(1,1)-GJR(1,1) are all significant, but with PBRA, only in the long run. In addition, at the univariate level, most of the estimates of the asymmetric effects, in which negative shocks have a greater impact on volatility than so positive shocks of a similar magnitude, are significant, except for TOT, LKOH and SNGS. The univariate estimates of the conditional volatilities, and the structural properties of both univariate models, namely the second moment and log-moment conditions, based on WTI crude futures returns and oil company stock returns, are satisfied empirically, so that statistical inference is valid.

[Insert Table 1 here]
The estimates of the constant conditional correlations between WTI crude oil futures returns and oil company stock returns, and the Bollerslev-Wooldridge (1992) robust t-ratios using the CCC model based on estimating univariate GARCH(1,1) models, are presented in Table 1. For the ten oil company stock returns, there are ten conditional correlations. The highest estimated constant conditional correlation is 0.334 between the standardized shocks to the volatilities in WTI crude oil futures and COP returns, and the lowest is 0.065 between the standardized shocks to the volatilities in WTI crude oil futures and SNGS returns. These estimated constant conditional correlations are reasonably low.

[Insert Table 2 here]

The corresponding multivariate estimates for the VARMA(1,1)-GARCH(1,1) and VARMA(1,1)-AGARCH(1,1) models using the BHHH (Berndt, Hall, Hall and Hausman) algorithm, and the Bollerslev-Wooldridge (1992) robust t-ratios, are reported in Tables 3 and 4, respectively. The estimates of the conditional mean for VARMA-GARCH are available from the authors upon request. In Panels 2a-2j, the ARCH and GARCH effects for WTI futures returns and oil company stock returns are statistically significant in the conditional volatilities for both the WTI futures returns and oil company stock returns. Interestingly, Table 3 shows there is no evidence of volatility spillovers in either one direction or two directions (namely, interdependence). Thus, all pairs of WTI futures returns and oil company stock returns are affected only by the short run and long run shocks in their own returns.

[Insert Table 3 here]

The results of VARMA-AGARCH in Panels 3a-3j mirror those in Panels 2a-2j. As in Table 2, the estimates of the conditional mean for VARMA-AGARCH are available from the authors on request. Surprisingly, in Panels 3a-3j, the coefficients of volatility spillovers are all statistically insignificant. Therefore, each pair of returns in the portfolio is affected only by their own previous short run (or ARCH) and long run (or GARCH) shocks, but the pairs WTI_ENI WTI_PBRA and WTI_SNGS hold only in the long run. The estimates of the conditional variances also show that asymmetric effects are evident in all cases, thereby suggesting that VARMA-GARCH is superior to VARMA-AGARCH.
5. Conclusion

The empirical analysis in the paper examined the volatility spillovers between the returns to crude oil futures and oil company stocks using alternative multivariate GARCH model, namely CCC, VARMA-GARCH and VARMA-AGARCH. This paper investigated the WTI crude oil futures returns and stock returns of ten oil companies, comprising the group of “supermajor” oil companies, namely Exxon Mobil, Royal Dutch Shell, Chevron Corporation, ConocoPhillips, BP and Total S.A., and four other large oil and gas companies, namely Petrobras, Lukoil, Surgutneftegas, and Eni S.p.A.

The empirical results showed that the conditional correlations between WTI crude oil futures returns and oil company stock returns in the CCC model were very low. The VARMA-GARCH and VARMA-AGARCH results showed that there were no spillover effects between any pairs of returns series. The evidence of asymmetric effects of negative and positive shocks of equal magnitude on the conditional variances suggested that VARMA-AGARCH was superior to VARMA-GARCH, and that both were superior to CCC.
References


Table 1. Conditional correlations from CCC between returns on WTI crude oil futures and oil company stocks

<table>
<thead>
<tr>
<th>Variable</th>
<th>BP</th>
<th>COP</th>
<th>CVX</th>
<th>ENI</th>
<th>LKOH</th>
<th>PBRA</th>
<th>RDS</th>
<th>SNGS</th>
<th>TOTAL</th>
<th>XOM</th>
</tr>
</thead>
<tbody>
<tr>
<td>WTI</td>
<td>0.172</td>
<td>0.334</td>
<td>0.314</td>
<td>0.115</td>
<td>0.102</td>
<td>0.164</td>
<td>0.119</td>
<td>0.065</td>
<td>0.149</td>
<td>0.255</td>
</tr>
</tbody>
</table>

Notes: (1) The two entries for each parameter are their respective estimate and the Bollerslev and Wooldridge (1992) robust t-ratios.
(2) Entries in bold are significant at the 5% level.
Table 2. VARMA-GARCH Conditional Correlations

<table>
<thead>
<tr>
<th>Panel</th>
<th>Variables</th>
<th>( \alpha )</th>
<th>( \alpha_{WTI} )</th>
<th>( \alpha_{BP} )</th>
<th>( \beta_{WTI} )</th>
<th>( \beta_{BP} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2a.</td>
<td>WTI_BPs</td>
<td>0.046</td>
<td>0.070</td>
<td>0.001</td>
<td>0.920</td>
<td>-0.003</td>
</tr>
<tr>
<td></td>
<td>BP</td>
<td>0.136</td>
<td>0.032</td>
<td>0.058</td>
<td>-0.017</td>
<td>0.912</td>
</tr>
<tr>
<td>2b.</td>
<td>WTI_COP</td>
<td>0.046</td>
<td>0.061</td>
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<td>0.928</td>
<td>0.003</td>
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<tr>
<td></td>
<td>COP</td>
<td>0.134</td>
<td>0.016</td>
<td>0.058</td>
<td>0.004</td>
<td>0.908</td>
</tr>
<tr>
<td>2c.</td>
<td>WTI_CVX</td>
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<td>0.069</td>
<td>0.002</td>
<td>0.913</td>
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</tr>
<tr>
<td></td>
<td>CVX</td>
<td>0.143</td>
<td>0.012</td>
<td>0.063</td>
<td>0.003</td>
<td>0.907</td>
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<tr>
<td>2d.</td>
<td>WTI_ENI</td>
<td>0.024</td>
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<td>-0.004</td>
<td>0.916</td>
<td>0.005</td>
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<tr>
<td></td>
<td>ENI</td>
<td>0.141</td>
<td>0.034</td>
<td>0.055</td>
<td>-0.007</td>
<td>0.908</td>
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<td>WTI_LKOH</td>
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<td>LKOH</td>
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<td>0.062</td>
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<td>2f.</td>
<td>WTI_PBRA</td>
<td>0.155</td>
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<td>0.909</td>
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<tr>
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<td>PBRA</td>
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<td>2g.</td>
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<td>0.021</td>
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<td>RDS</td>
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<td>0.100</td>
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<tr>
<td>2h.</td>
<td>WTI_SNGS</td>
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<td></td>
<td>SNGS</td>
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<td>-0.024</td>
<td>0.079</td>
<td>0.040</td>
<td>0.911</td>
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<tr>
<td>2i.</td>
<td>WTI_TOTAL</td>
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<td>0.020</td>
<td>0.924</td>
<td>-0.008</td>
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<td>TOTAL</td>
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<td>1.82E-05</td>
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<td>2j.</td>
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<tr>
<td></td>
<td>XOM</td>
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<td>-0.001</td>
<td>0.071</td>
<td>0.001</td>
<td>0.909</td>
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</tbody>
</table>

Notes: (1) The two entries for each parameter are their respective estimate and the Bollerslev and Wooldridge (1992) robust t-ratios.
(2) Entries in bold are significant at the 5% level.
Table 3. VARMA-AGARCH Conditional Correlations

<table>
<thead>
<tr>
<th>Panel</th>
<th>Symbol</th>
<th>Parameter 1</th>
<th>Parameter 2</th>
<th>Parameter 3</th>
<th>Parameter 4</th>
<th>Parameter 5</th>
<th>Parameter 6</th>
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</thead>
<tbody>
<tr>
<td>3a</td>
<td>WTI_BBP</td>
<td>$\sigma$</td>
<td>$\alpha_{WTI}$</td>
<td>$\alpha_{BP}$</td>
<td>$\gamma$</td>
<td>$\beta_{WTI}$</td>
<td>$\beta_{BP}$</td>
</tr>
<tr>
<td>WTI</td>
<td>0.137</td>
<td>0.036</td>
<td>0.031</td>
<td>0.037</td>
<td>0.915</td>
<td>-0.017</td>
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<tr>
<td>BP</td>
<td>0.049</td>
<td>0.001</td>
<td>0.044</td>
<td>0.047</td>
<td>-0.003</td>
<td>0.921</td>
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<td>3b</td>
<td>WTI_COP</td>
<td>$\sigma$</td>
<td>$\alpha_{WTI}$</td>
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<td>$\gamma$</td>
<td>$\beta_{WTI}$</td>
<td>$\beta_{COP}$</td>
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<tr>
<td>WTI</td>
<td>0.135</td>
<td>0.038</td>
<td>0.016</td>
<td>0.032</td>
<td>0.912</td>
<td>0.002</td>
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<tr>
<td>COP</td>
<td>0.060</td>
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<td>0.033</td>
<td>0.048</td>
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<tr>
<td>3c</td>
<td>WTI_CVX</td>
<td>$\sigma$</td>
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<td>$\gamma$</td>
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<td>$\beta_{CVX}$</td>
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<td>-0.002</td>
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Notes: (1) The two entries for each parameter are their respective estimate and the Bollerslev and Wooldridge (1992) robust $t$-ratios. (2) Entries in bold are significant at the 5% level.
Figure 1

Returns of daily futures prices for WTI
Figure 2
Returns of daily oil company stock prices